

PART A

I. Answer ALL the multiple-choice questions

1 x 15 = 15

1. Which of the following is not correct?
 - a) Set of rational numbers is a subset of real number
 - b) $\{x : x \text{ is an even natural number}\}$ is subset of $\{x : x \text{ is an integer}\}$
 - c) If A is set of all prime divisors of 56, and B is set of all divisors of 56, then B is subset of A
 - d) $\{1, 5, 9\} \subset \{1, 3, 5, 7, 9\}$
2. If $A = \{1, 2, 3\}$ and $B = \{5, 6\}$, then number of relations from A to B is
 - a) 6
 - b) 36
 - c) 64
 - d) 128
3. The angle 1π in degrees is
 - a) 1
 - b) 180
 - c) 360
 - d) 0
4. The imaginary part of $4 - 5i$ is
 - a) -5
 - b) $-5i$
 - c) 5
 - d) $5i$
5. The solution set for $\frac{3-2x}{6} \leq \frac{x}{6} + 5$ is
 - a) $(9, \infty)$
 - b) $(-\infty, 9)$
 - c) $[9, \infty)$
 - d) $(-9, \infty)$
6. If ${}^nC_9 = {}^nC_8$, then value of n is
 - a) 10
 - b) 15
 - c) 14
 - d) 21
7. The sum of terms in the expansion of $(x+a)^{10} + (x-a)^{10}$ is
 - a) 22
 - b) 6
 - c) 21
 - d) 11
8. If $-\frac{2}{7}, x, -\frac{7}{2}$ are in G.P., then the common ratio is
 - a) 1
 - b) ± 1
 - c) 2
 - d) ± 2
9. A line passes through $(2, -2)$ and is parallel to y-axis, then the equation of the line is
 - a) $y=2$
 - b) $x=2$
 - c) $y=-2$
 - d) $x=-2$
10. In which quadrant the parabola $x^2 = -4ay$ doesn't exist is
 - a) I, II
 - b) II, III
 - c) III, IV
 - d) I, IV
11. The eccentricity of the ellipse $9x^2 + 25y^2 = 225$ is
 - a) $3/4$
 - b) $4/5$
 - c) $9/16$
 - d) $3/5$
12. The octant in which the point $(1, 2, -5)$ lie is
 - a) V
 - b) VI
 - c) VII
 - d) VIII
13. The value of $\lim_{x \rightarrow 3} \frac{x^4 - 81}{2x^2 - 5x - 3}$ is
 - a) $\frac{7}{108}$
 - b) ∞
 - c) $\frac{108}{7}$
 - d) 0
14. The median of the data 3, 9, 5, 3, 7, 12, 10, 18, 4, 7, 19, 21 is
 - a) 10
 - b) 8
 - c) 9
 - d) 9.5
15. The number of simple events corresponding to the sample space "two dice are rolled at once" is
 - a) 6
 - b) 36
 - c) $1/18$
 - d) 12

II. Fill in the blanks by choosing the appropriate answer from those given in the bracket. 5 x 1 = 5**(10, 3, 1, -1, 5, 0)**

16. If $A = \{2, 4, 6, 8\}$, and $B = \{2, 3, 5, 7\}$ the $n(A-B)$ is _____
17. If $3 - x > 2$, when x is a natural number. The number of values of x is _____
18. If ${}^n P_3 = 60$ then ${}^n C_3$ is _____
19. The value of y for which the points $(1, y), (2, -1)$ and $(4, 5)$ are collinear will be _____
20. The derivative of $f(x) = 3 - x$ at $x = 1$ is _____

PART B**III. Answer any SIX questions:****6 x 2 = 12**

21. If $A = \{2, 4, 6, 8, 10\}$, $B = \{1, 4, 8\}$ and $C = \{4, 8, 12\}$, find $A \cap (B - C)$
22. Find the radius of the circle in which a central angle is 60° intercepts an arc of length 37.4 cm.
23. Prove that $\cos\left(\frac{\pi}{4} - x\right)\cos\left(\frac{\pi}{4} - y\right) - \sin\left(\frac{\pi}{4} - x\right)\sin\left(\frac{\pi}{4} - y\right) = \sin(x + y)$
24. Express the complex number $(1 - i)^4$ in $a + ib$ form.
25. How many three digit even numbers can be made using the digits 1, 2, 3, 4, 6, and 7, if no digit is repeated?
26. Using binomial theorem evaluate $(98)^4$.
27. The sum of three terms of a G.P. is $\frac{13}{12}$ and their product is -1. Find the common ratio and the terms.
28. Find the equation of the circle with centre $(1, 1)$ and radius $\sqrt{2}$
29. If $P(A) = \frac{2}{3}$ and $P(B) = \frac{1}{5}$, find $P(A \text{ or } B)$, if A and B are mutually exclusive.

PART C**IV. Answer any SIX questions:****6 x 3 = 18**

30. If $U = \{1, 2, 3, 4, 5, 6, 7, 8\}$, $A = \{2, 3, 5, 7\}$ and $B = \{2, 4, 6, 8\}$ verify $(A \cup B)' = A' \cap B'$
31. Draw Venn diagrams for the (i) $A \cup B$ (ii) $A - B$ (iii) $(A \cap B)'$
32. Show that $\cos 2x = \frac{1 - \tan^2 x}{1 + \tan^2 x}$
33. If $(x + iy)^3 = u + iv$ then show that $\frac{u}{x} + \frac{v}{y} = 4(x^2 - y^2)$
34. Solve the inequality and show the solution on the number line $\frac{3x - 4}{2} \geq \frac{x + 1}{4} - 1$
35. Using binomial theorem, show that $9^{n+1} - 8n - 9$ is divisible by 64, whenever n is a positive integer.
36. If p is the length of perpendicular from the origin to the line whose intercepts on the axes are a and b , then show that $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{p^2}$
37. Show that the points $A(1, 2, 3)$, $B(-1, -2, -1)$, $C(2, 3, 2)$ and $D(4, 7, 6)$ are vertices of parallelogram and not of rectangle.
38. Find the derivative of x^n w.r.t x from first principles.

PART D**V. Answer any FOUR questions:****4 x 5 = 20**

39. Define polynomial function. If the function $f : \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = x^3$, draw the graph of it. Also write its domain and range.
40. Prove that $\frac{\cos 4x + \cos 3x + \cos 2x}{\sin 4x + \sin 3x + \sin 2x} = \cot 3x$
41. State and prove binomial theorem.
42. Derive the expression for the perpendicular distance between the point (x_1, y_1) and a line $Ax + By + C = 0$
43. Prove geometrically $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$
44. Find the variance and standard deviation for the following data:

Classes	0-10	10-20	20-30	30-40	40-50
Frequencies	5	8	15	16	6

45. Find the probability that when a hand of 7 card is drawn from a well shuffled deck of 52 cards, it contains (i) all kings (ii) 3 kings (iii) at least 3 kings

PART E**VI. Answer the following question.**

46. Prove geometrically $\cos(x + y) = \cos x \cos y - \sin x \sin y$ and hence prove that $\cos 75^\circ = \frac{\sqrt{3}-1}{2\sqrt{2}}$

OR**6**

Define and derive the equation of parabola in the standard form $y^2 = 4ax$ and find the latus rectum of the parabola $y^2 = 8x$

47. Find the derivative of $f(x) = \frac{x + \cos x}{\tan x}$ with respect to x .

OR**4**

Find the sum of the series up to n terms $7+77+777+\dots\dots$
